

All pair shortest path
using Rkleene algorithm

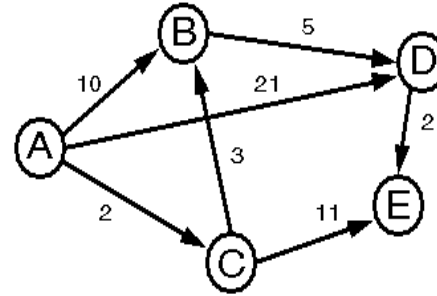
-Abhyodaya

All pair shortest path

- Floyd Warshall Algorithm.
- Dijkstra.
- Recursive Kleene Algorithm.

(exploits data locality).

(source: R-Kleene: A High-Performance Divide-and-Conquer Algorithm for the All-Pair Shortest Path for Densely Connected Networks)



RKleene

- It is a divide and conquer algorithm.
- Based on matrix multiplication.

Replaced operations

Multiply with **Add**

Addition with **Min**

```
R-Kleene (J) {
  /*   | A  B | */
  /* J = | C  D | */

  1:  A = R-Kleene (A) ;
  2:  B += A*B;
  3:  C += C*A;
  4:  D += C*B;

  5:  D = R-Kleene (D) ;
  6:  B += B*D;
  7:  C += D*C;
  8:  A += B*C;
}
```

(Source : R-Kleene: A High-Performance Divide-and-Conquer Algorithm for the All-Pair Shortest Path for Densely Connected Networks)

Rkleene

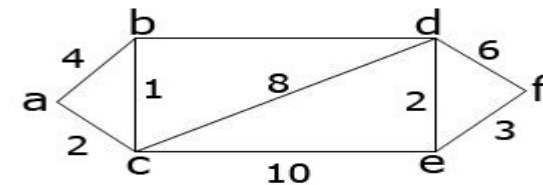
- **Steps**

- a) Division of adj mat to 4 components
- b) Call Rkleene on all 4 parts.
- c) Perform MM on results of 4 parts.

- **MM operation explained**

source img : dijkstra eg <http://programming-technique.blogspot.com/>)

w(u,v)	a	b	c	d	d	f
a	0	4	2	INF	INF	INF
b	4	0	1	5	INF	INF
c	2	1	0	8	10	INF
d	INF	5	8	0	2	6
e	INF	INF	10	2	0	3
f	INF	INF	INF	6	3	0



Consider Example for . $B += A*B$

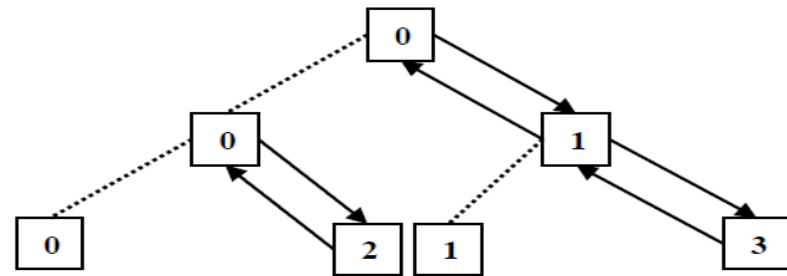
Initial (a,d) = INFINITE

$$(a,d) = \min((a,d), ((a,c) + (c,d))) \\ = \min(\text{INFINITE} + (2+8)) = 10$$

MPI RKleene

- Assumption : all nodes have access to input graph data.
- MPI_Send to send matrix indexes to work on.
- MPI_Recv to receive data from process.
- Partition algorithm needed for MPI process as number of process is fixed.

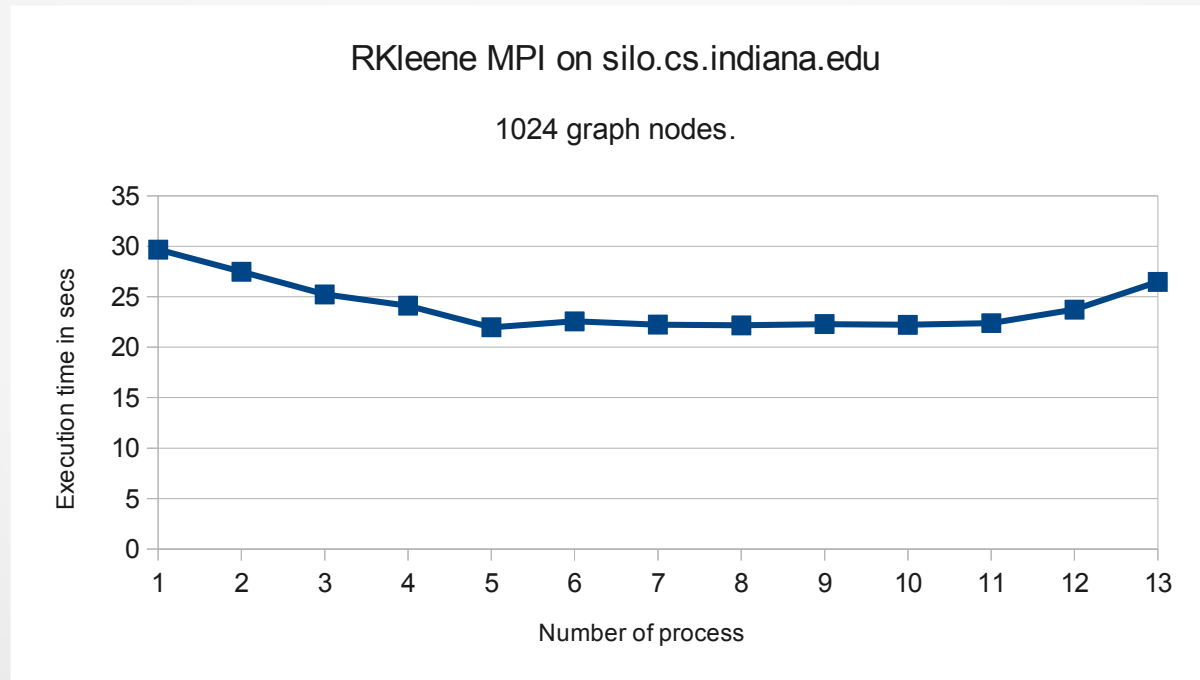
Source : Shared Memory, Message Passing, and Hybrid Merge Sorts Standalone and Clustered SMPs.



```
int helper_rank = my_rank + pow(2, level);
```

Initial test MPI Rkleene.

- Initial test with 1024 graph nodes on silo.cs.indiana.edu.





Thanks